

# 第一届5G算法创新大赛

## ——SCMA

现场宣讲&答疑会

2015年7月16日

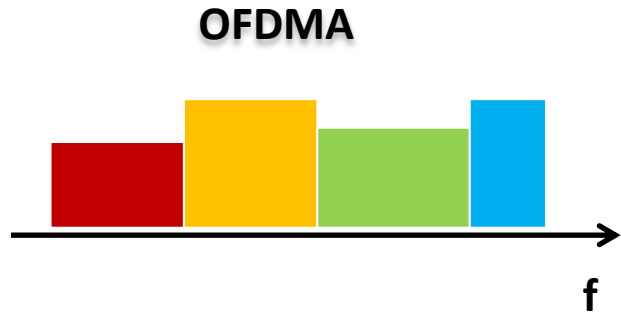
# Outline

- **Warm Up Introductions**
- **The System You are Going to Implement**
- **Second Look at SCMA Encoder/Decoder**
- **Some Other Magic about SCMA**
- **Real-time SCMA Demo in Field**

What is SCMA, and why SCMA

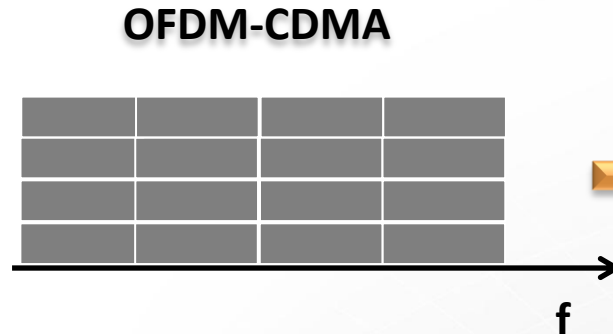
# WARM UP INTRODUCTIONS

# From OFDMA to SCMA



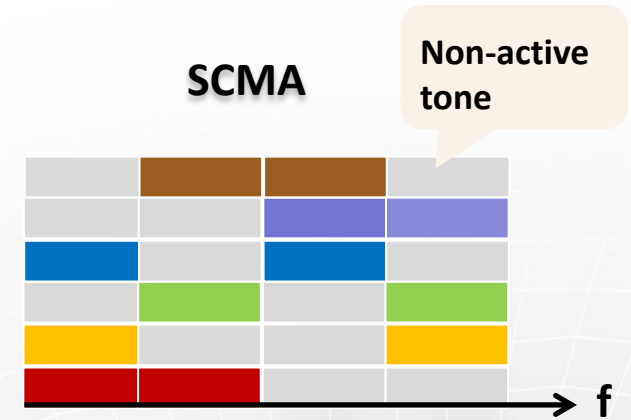
## Orthogonal multi-user multiplexing

- Users occupy orthogonal resources for communication
- Easy to implement (single user detection)
- Number of connections limited by the number of physical resource blocks that can be scheduled



## Non-orthogonal multi-user multiplexing

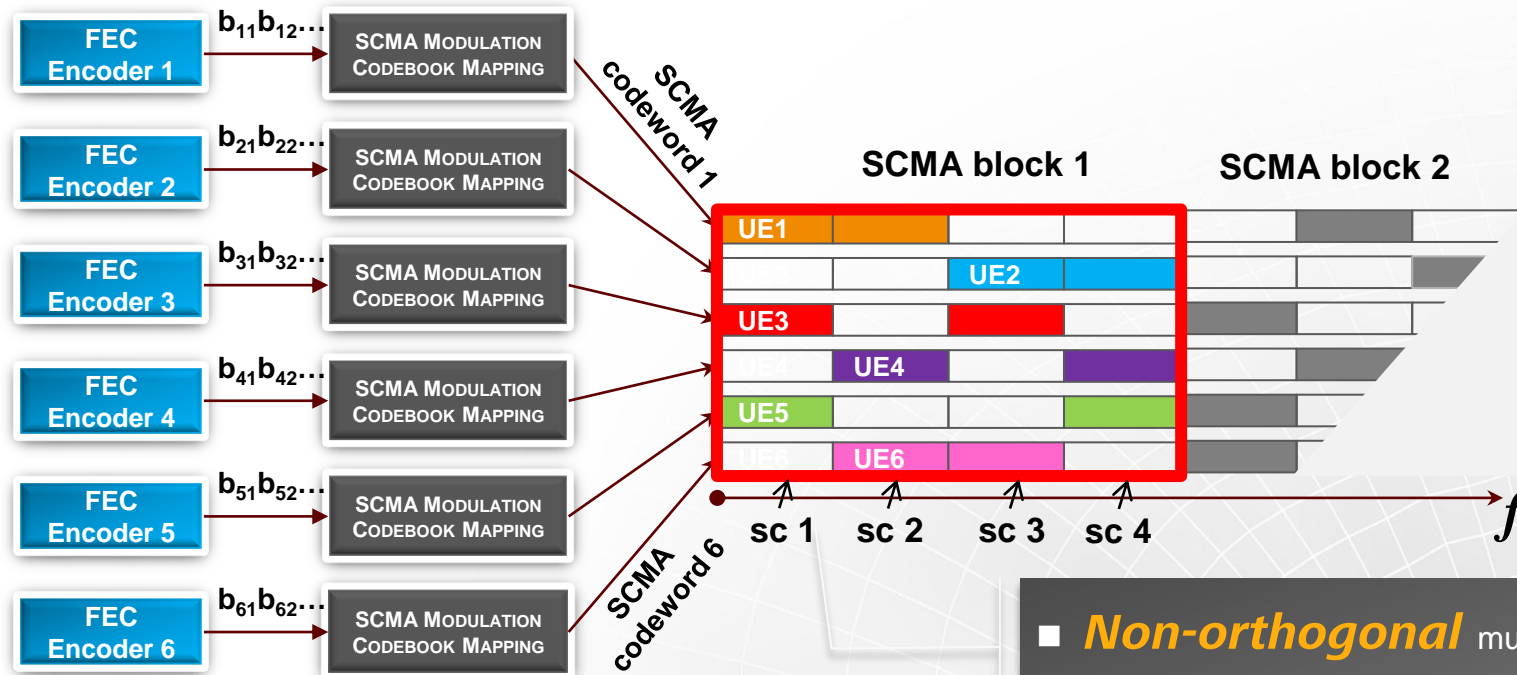
- Users occupy the same resource blocks using CDMA
- Non-practically high multi-user joint detection complexity
- Limited number of concurrent users due to limited sequences
- Better coverage due to spreading gain



## Overloaded multi-user multiplexing

- Users occupy the same resource blocks in a low density way
- Affordable low multi-user joint detection complexity
- Less collision even for large number of concurrent Users
- Better coverage due to spreading gain

# SCMA (Sparse Code Multiple Access)



## A new frequency domain non-orthogonal waveform

- ❑ Input bits are directly mapped to codewords and spread over multiple sub-carriers
- ❑ Codewords can be assigned to same UE or different UEs

- **Non-orthogonal** multiplexing of code layers
- **Over-Loading** to increase overall rate and connectivity
- **Sparsity** to limit Rx complexity for detection
- **Spreading** for robust link-adaptation, coverage
- **Multi-dimensional** codewords with shaping/coding gain

Simplified system, module interface definition, configuration parameters

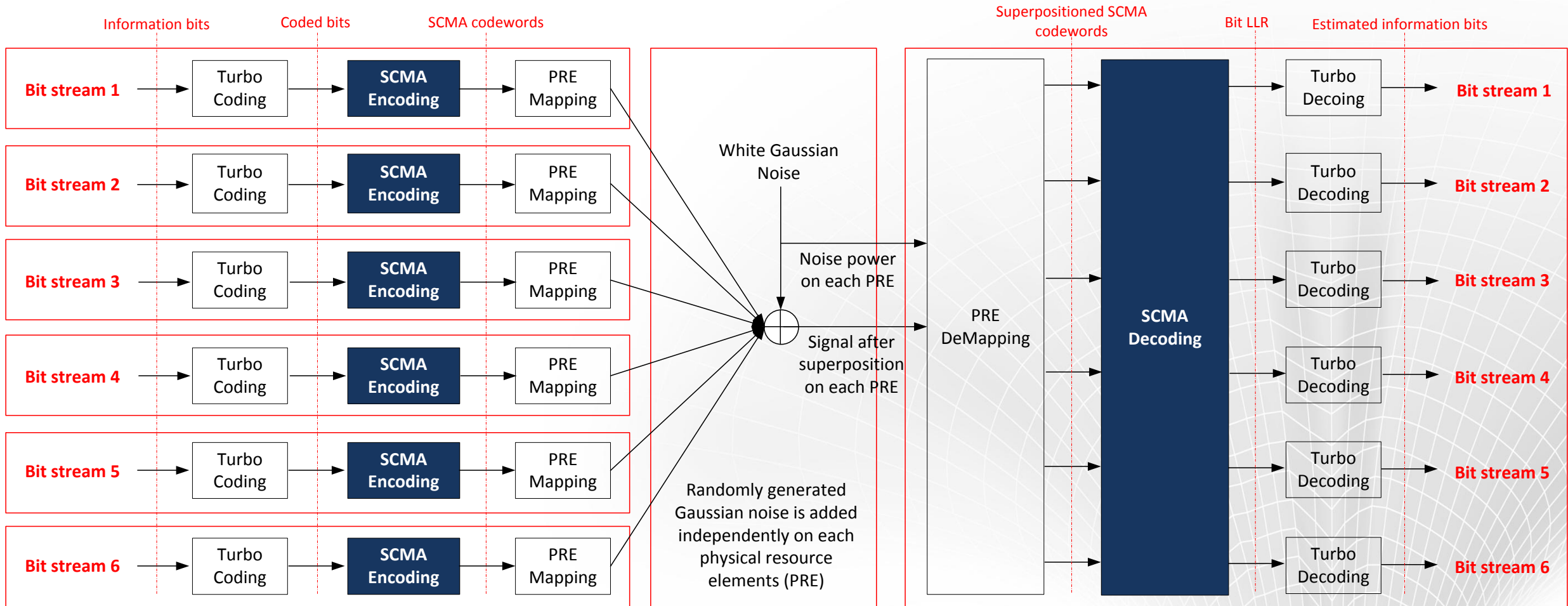
# **THE SYSTEM YOU ARE GOING TO IMPLEMENT**

# Simplified Uplink SCMA System to be Implemented

Simplified Transmitter Side Representing 6 Users, each taking one layer of the SCMA codebook, namely  $CB_i$  for user  $i$

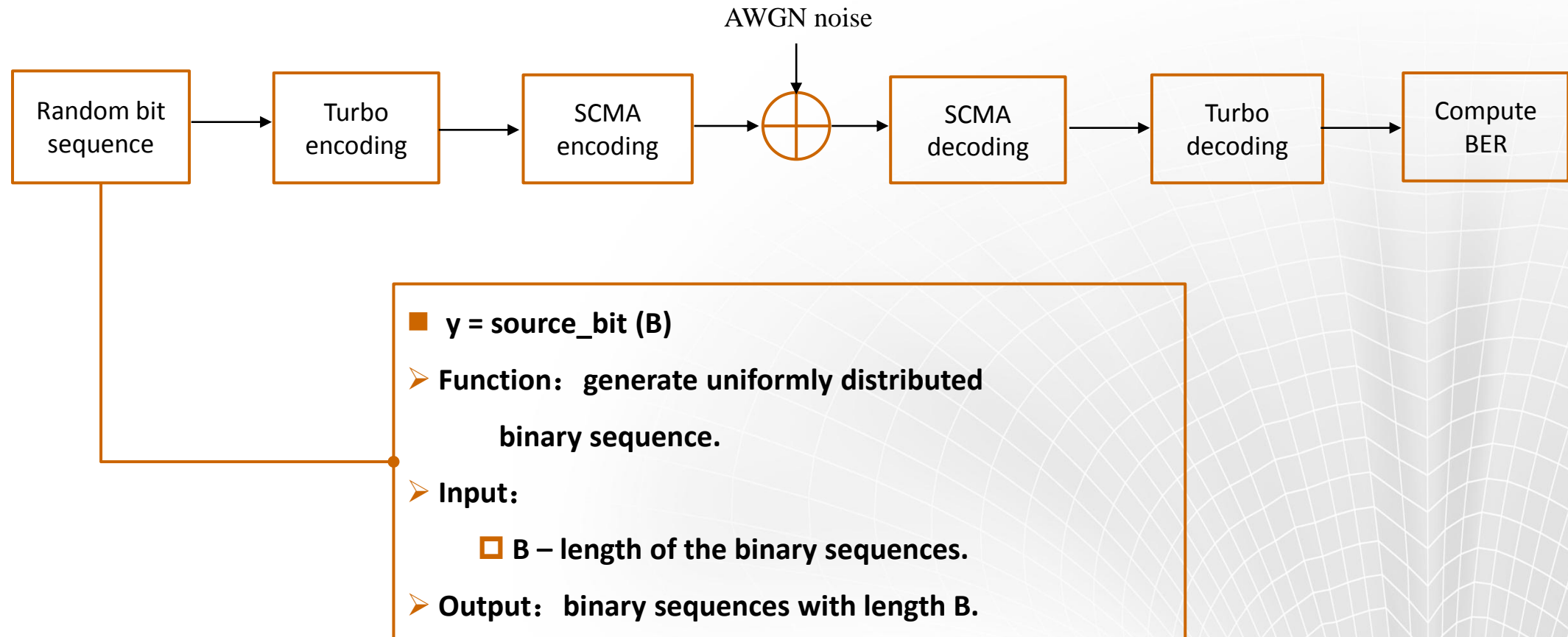
Simplified Communication Channel

Simplified Receiver Side Representing Base Station, with joint multi-user detection using MPA algorithm



\* Turbo coding and decoding can be replaced by other forward error correction (FEC) channel coding/decoding modules.

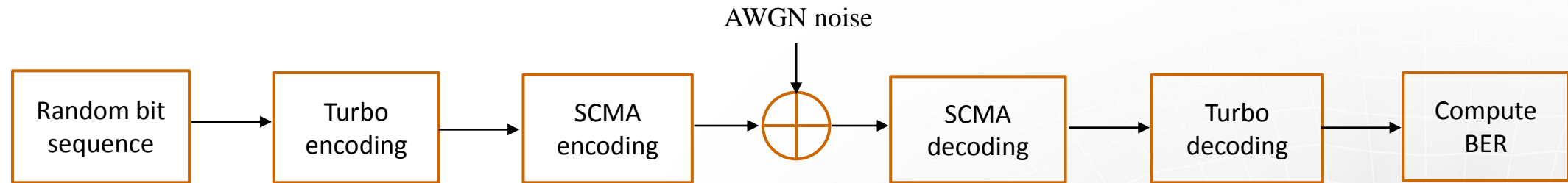
# Simplified Uplink SCMA System to be Implemented



Note: Every module is performed for data streams of 6 users.

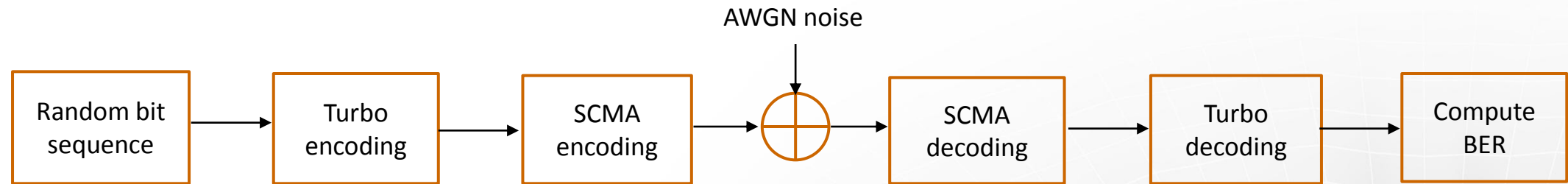


# Simplified Uplink SCMA System to be Implemented



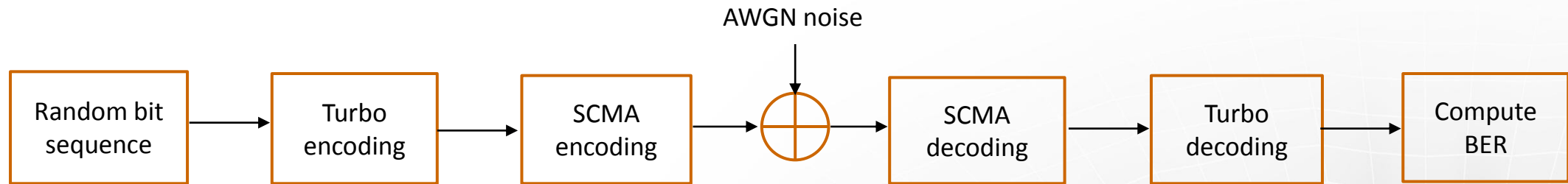
- $y = \text{turbo\_encoding}(\text{source\_bit}, R)$
- **Function:** to perform Turbo encoding.
- **Input:**
  - **source\_bit** – binary sequence to be encoded;
  - **R** – coding rate.
- **Output:** Turbo encoded bits with length  $N = B/R$ .

# Simplified Uplink SCMA System to be Implemented



- $y = \text{scma\_encoding}(\text{encode\_seq}, \text{CB})$
- **Function:** bit sequences from 6 users are SCMA encoded according to specified codebooks.
- **Input:**
  - `encode_seq` – encoded bit streams of 6 layers;
  - `CB` – codebooks for each layer.
- **Output:** superposed symbols to be transmitted.

# Simplified Uplink SCMA System to be Implemented



■  $y = \text{scma\_decoding}(r, \text{CB}, H, N_0)$

➤ **Function:** to recover the bit information of each layer

➤ **Input:**

▣  $r$  – received signals from the channel;

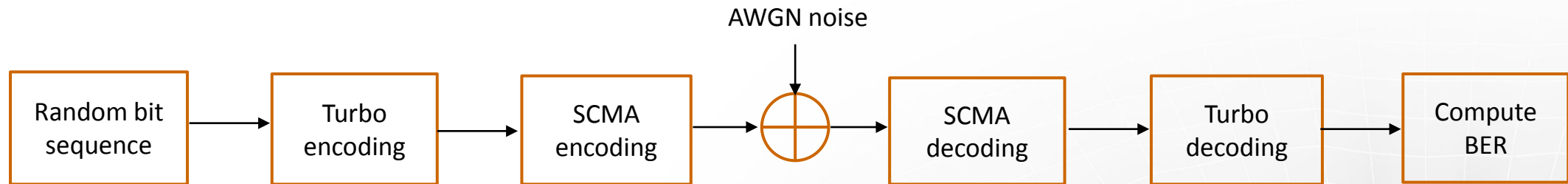
▣  $\text{CB}$  – codebooks of each layer;

▣  $H$  – channel state information;

▣  $N_0$  – noise information.

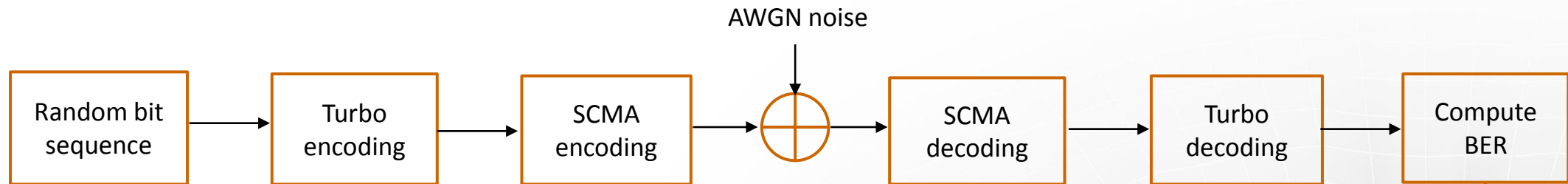
➤ **Output:** LLRs of encoded bits.

# Simplified Uplink SCMA System to be Implemented



- $y = \text{turbo\_decoding}(\text{LLR}, \text{rate})$
- **Function:** to perform Turbo decoding.
- **Input:**
  - LLR – bit LLRs output from SCMA decoder;
  - rate – channel coding rate.
- **Output:** recovered source bit sequence.

# Simplified Uplink SCMA System to be Implemented



■  $y = \text{err\_check}(\text{source\_bit}, \text{decode\_bit})$

➤ **Function:** to calculate the BLER

➤ **Input:**

▣ **source\_bit** – source bits of each user;

▣ **decode\_bit** – recovered bits of each user;

➤ **Output:** average BER.

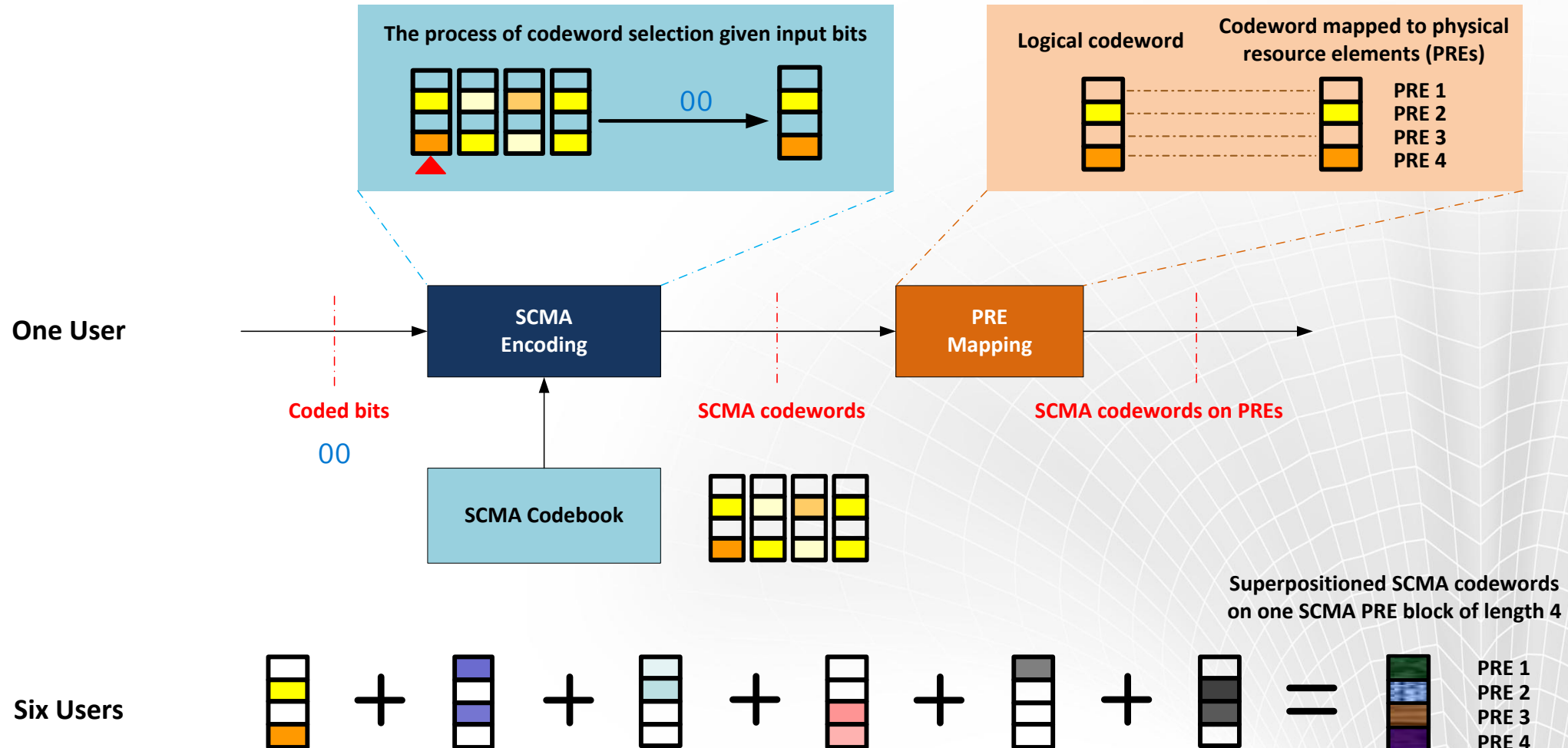
# System Configuration Parameters for Implementation

Parameter Categories	Related Variables	Typical value	Description
SCMA Codebook	V	6	6 variable nodes (VN), number of data layers
	F	4	4 function nodes (FN), number of physical resources
	d <sub>f</sub>	3	Each FN is connected to 3 VNs
	d <sub>v</sub>	2	Each VN is connected to 2 FNs
	M	4	Number of codeword in each codebook
	CB <sub>i</sub>	F-by-M matrix	Codebook for one SCMA data layer, given
Turbo Coding	R	1/2	Coding rate, defined as the ratio of information bits over coded bits
SCMA decoding	N <sub>iter</sub>	3 ~ 15	Number of iterations in MPA
	H <sub>n</sub>	{1}	Channel gain, in the white Gaussian noise only case, H <sub>n</sub> ={h <sub>n,k</sub> }= {1}
	APP <sub>i</sub>	1/M	A prior probability of codeword i, assuming equal probability 1/M
System Scale	B	125 bytes = 1000 bits	Total number of information bits, randomly generated
	N	B / R = 2000 bits	Total number of coded bits after Turbo coding
	L	L = F * N/log <sub>2</sub> (M) = 4000	Total number of physical resource units

MPA Algorithm, complexity reduction hints

# SECOND LOOK AT SCMA ENCODER/DECODER

# How to Do SCMA Encoding with SCMA Codebook



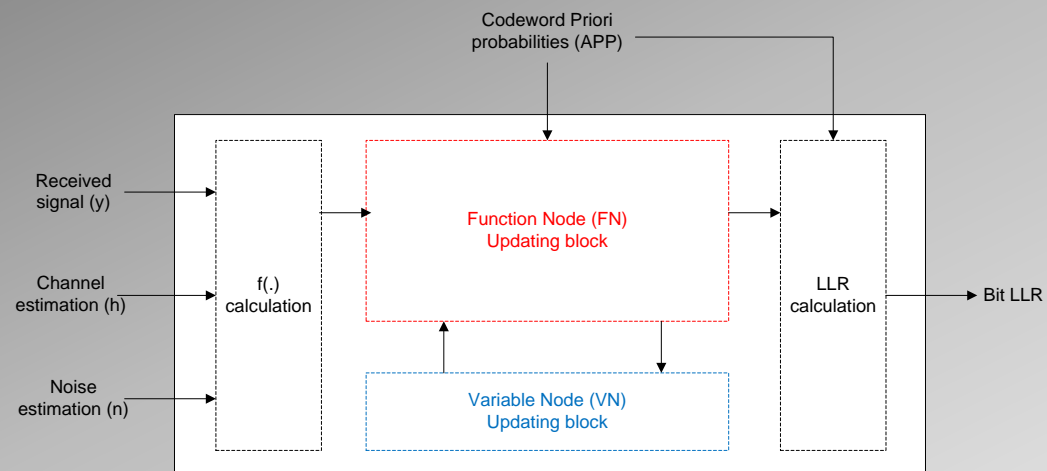


# How to Do SCMA Decoding with MPA Algorithm

## Selection of SCMA Decoder

- The optimal multi-user detection can be done by using the maximum joint a posteriori probability (MAP) detection with excessive search – **non-practical complexity**
- With the low density spreading structure employed in SCMA, we can derive near ML performance multi-user detection with **message passing algorithm (MPA)** – **affordable complexity**

## Diagram for Message Passing Algorithm



## MPA Decoder (Performed for each SCMA block)

Initial calculation of the conditional probability

Iterative message passing along edges

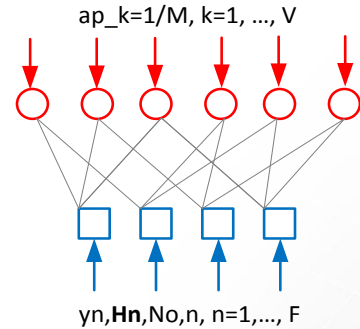
1. **FN updates and message passing to VN**
2. **VN updates and message passing to FN**

$N_{\text{iter}}$  iterations?

Output the final guess of the codeword of each data layer at VN node and change the probability to bit LLR for channel decoder

# How to Do SCMA Decoding with MPA Algorithm

Parameters	Description of the parameters
$y_n, n=1, \dots, F$	Received signal as input to the MPA decoder on resource n
$m_k, k=1, \dots, V$	Codeword selected by layer k, $m_k = 1, \dots, M$
$N_{0,n}, n=1, \dots, F$	Noise power estimation on physical resource n
$C_{k,n}(m_k)$	The constellation symbol of VN node k on physical resource n when using codeword $m_k$
$H_n = \{h_{n,k}\}$	Channel gain of user k on physical resource n
$A_{p,k}, k=1, \dots, V$	A prior probability of codeword k, assuming equal probability $1/M$
LLR <sub>k,b</sub>	logarithm of the likelihood ratio of layer k bit b
N_iter	Number of iterations in the MPA



## Step 1: Initial calculation of the conditional probability

- For each function node FN, calculate the  $f_n()$  function, which is the set of all possible residual signals given the known or estimated channel  $h_{n,k}$  and the assumed transmitted codeword  $C_{k,n}(m_k)$
- When  $d_f = 3$ , as in the example, for each FN node n, there are  $M^3$  combinations of transmitted signals, so there are in total  $F^3 M^3$  values to store for  $f()$  function calculation

$$f_n(y_n, m_1, m_2, m_3, N_{0,n}, H_n) = \frac{-1}{N_{0,n}} \left\| y_n - (h_{n,1} C_{1,n}(m_1) + h_{n,2} C_{2,n}(m_2) + h_{n,3} C_{3,n}(m_3)) \right\|^2$$

$$m_1 = 1, \dots, M \quad m_2 = 1, \dots, M \quad m_3 = 1, \dots, M \quad n = 1, \dots, F$$

- $\Phi_n()$  function is actually the conditional probability for given codeword combination, for Gaussian noise case, it is the exponential operation over  $f_n$  function, so the storage needed is the same

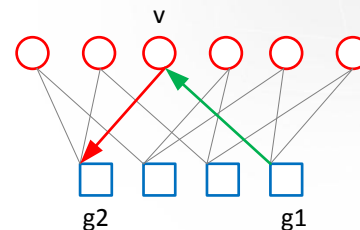
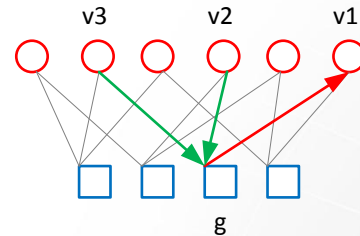
$$P(y_n | x_1, x_2, x_3) \text{ ----- } \Phi_n(y_n, m_1, m_2, m_3, N_{0,n}, H_n) = \exp(f_n(y_n, m_1, m_2, m_3, N_{0,n}, H_n))$$

- To prepare for the iterations, we assign the a prior probability for each codeword, which is assumed to be equal

$$P(x_1), P(x_2), P(x_3) \text{ ----- } I_{v_1 \rightarrow g}^{init}(m_1) = I_{v_2 \rightarrow g}^{init}(m_2) = I_{v_3 \rightarrow g}^{init}(m_3) = \frac{1}{M}$$

# How to Do SCMA Decoding with MPA Algorithm

Parameters	Description of the parameters
$y_n, n=1, \dots, F$	Received signal as input to the MPA decoder on resource n
$m_k, k=1, \dots, V$	Codeword selected by layer k, $m_k = 1, \dots, M$
$N_{0,n}, n=1, \dots, F$	Noise power estimation on physical resource n
$C_{k,n}(m_k)$	The constellation symbol of VN node k on physical resource n when using codeword $m_k$
$H_n = \{h_{n,k}\}$	Channel gain of user k on physical resource n
$A_{p,k}, k=1, \dots, V$	A prior probability of codeword k, assuming equal probability $1/M$
$LLR_{k,b}$	logarithm of the likelihood ratio of layer k bit b
$N_{iter}$	Number of iterations in the MPA



## Step 2: Iterative message passing along edges

### [FN update]: message passing from FN to its neighboring VNs

- FN node  $g$  passes updates obtained from extrinsic information to its neighboring VN nodes ( $g$  to  $v_1$ , information from  $v_2$  and  $v_3$  are extrinsic)
- The message passed to  $v_1$  contains the guess of what signal at  $g$  may be given all possibilities of  $v_1$

$$I_{g \rightarrow v_1}(m_1) = \sum_{m_2=1}^M \sum_{m_3=1}^M \Phi_n(y_n, m_1, m_2, m_3, N_{0,n}, H_n) (I_{v_2 \rightarrow g}(m_2) I_{v_3 \rightarrow g}(m_3)) \quad m_1 = 1, \dots, M$$

$$I_{g \rightarrow v_2}(m_2) = \sum_{m_1=1}^M \sum_{m_3=1}^M \Phi_n(y_n, m_1, m_2, m_3, N_{0,n}, H_n) (I_{v_1 \rightarrow g}(m_1) I_{v_3 \rightarrow g}(m_3)) \quad m_2 = 1, \dots, M$$

$$I_{g \rightarrow v_3}(m_3) = \sum_{m_1=1}^M \sum_{m_2=1}^M \Phi_n(y_n, m_1, m_2, m_3, N_{0,n}, H_n) (I_{v_1 \rightarrow g}(m_1) I_{v_2 \rightarrow g}(m_2)) \quad m_3 = 1, \dots, M$$

### [VN update]: message passing from VN to its neighboring FNs

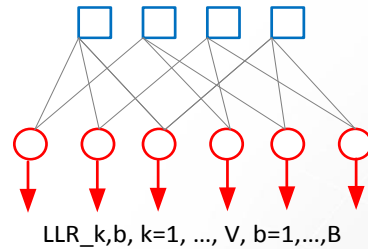
- VN node  $v$  passes updates obtained from extrinsic information to its neighboring FN nodes ( $v$  to  $g_2$ , information from  $g_1$  is extrinsic)
- In the  $d_v=2$  case, it is actually a "guess" swap at VN node

$$I_{v \rightarrow g_1}(m) = \text{normalize} (a_{p_v}(m) I_{g_2 \rightarrow v}(m)) \quad m = 1, \dots, M$$

$$I_{v \rightarrow g_2}(m) = \text{normalize} (a_{p_v}(m) I_{g_1 \rightarrow v}(m)) \quad m = 1, \dots, M$$

# How to Do SCMA Decoding with MPA Algorithm

Parameters	Description of the parameters
$y_n, n=1, \dots, F$	Received signal as input to the MPA decoder on resource n
$m_k, k=1, \dots, V$	Codeword selected by layer k, $m_k = 1, \dots, M$
$No_n, n=1, \dots, F$	Noise power estimation on physical resource n
$C_{k,n}(m_k)$	The constellation symbol of VN node k on physical resource n when using codeword $m_k$
$H_n = \{h_{n,k}\}$	Channel gain of user k on physical resource n
$Ap_k, k=1, \dots, V$	A prior probability of codeword k, assuming equal probability $1/M$
$LLR_{k,b}$	logarithm of the likelihood ratio of layer k bit b
$N_{iter}$	Number of iterations in the MPA



## Step 3: LLR output at variable node after $N_{iter}$ iterations

- After  $N_{iter}$  iterations, we shall output the guess at each VN node (for each data layer) as the detection results
- The guess at VN node  $v$  for codeword  $m$  is a chain product of all guesses from all its neighboring FN nodes and the a prior probability

$$Q_v(m) = ap_v(m) I_{g_1 \rightarrow v}(m) I_{g_2 \rightarrow v}(m) \quad m = 1, \dots, M$$

- After getting the probability guess of codeword at each layer, we then need to calculate the Log-Likelihood-Rate (LLR) for each coded bit, so that they can serve as the input for the turbo decoder (or any other channel decoder) directly after MPA

$$LLR_x = \log \left( \frac{P(b_x = 0)}{P(b_x = 1)} \right)$$

$$LLR_x = \log \left( \frac{\sum_{m: b_{m,x}=0} Q_v(m)}{\sum_{m: b_{m,x}=1} Q_v(m)} \right) = \log \left( \sum_{m: b_{m,x}=0} Q_v(m) \right) - \log \left( \sum_{m: b_{m,x}=1} Q_v(m) \right)$$

# Hints on Low Complexity MPA Receiver Design

- **Short-comings of the current MPA algorithm**

1. Though much lower complexity compared with the optimal MAP algorithm (thanks to the sparse structure of the SCMA codebook), it is still of high complexity for hardware
2. The  $\exp(\cdot)$  operations causes very large dynamic ranges and very high storage burden if using lookup table, which is not good news for hardware implementation

- **Hint 1: Change to LOG domain using Jacobi's logarithm**

1. After changing to Log domain,  $\exp(\cdot)$  operation disappears : **MPA -> MAX-Log MPA**

$$\log\left(\sum_{i=1}^N \exp(f_i)\right) \approx \max\{f_1, f_2, \dots, f_N\}$$

- **Hint 2: Optimize the calculations during iterations**

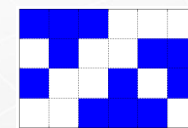
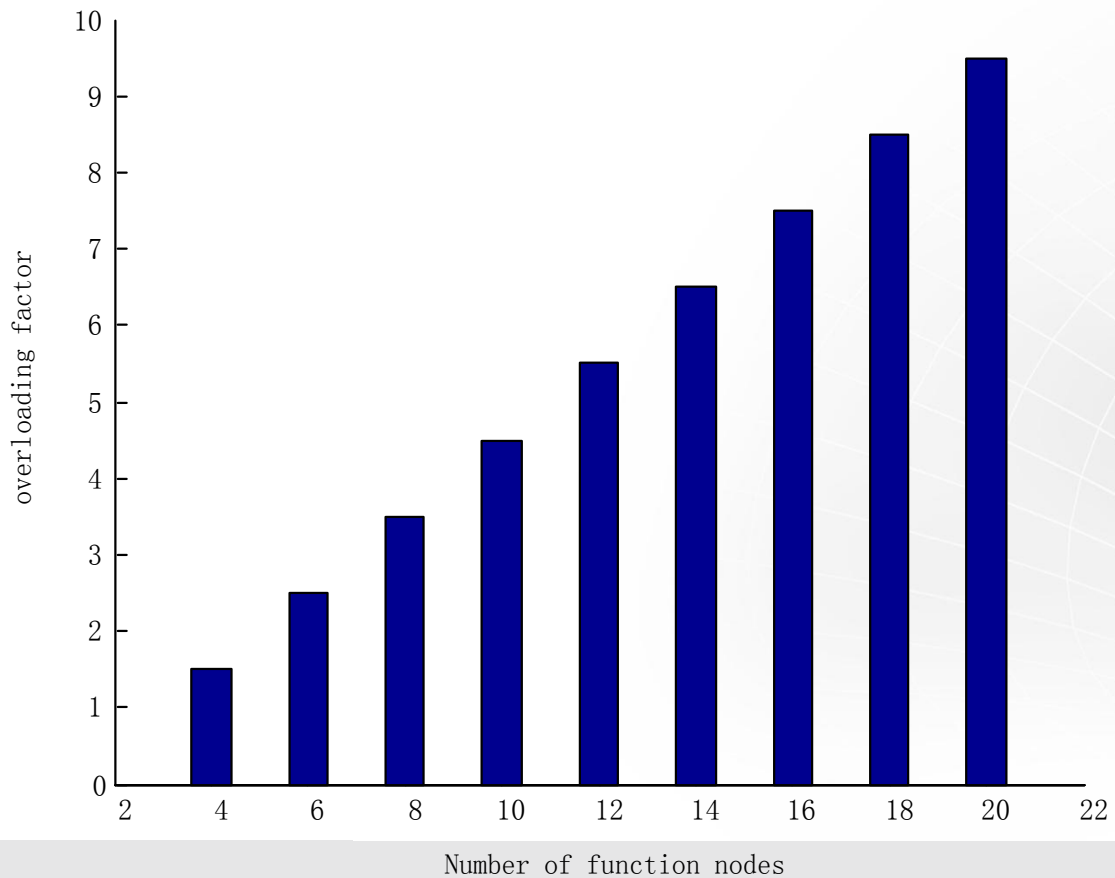
1. Try to optimize the order of iterations
2. Try to use as much as possible the common results in the calculation

**flexible overloading, Grant-free, Outer-loop Turbo MPA**

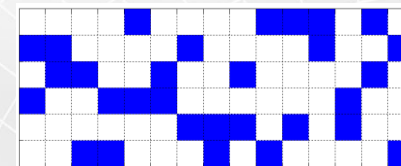
# **SOME OTHER MAGIC OF SCMA**

# Flexible overloading to support massive connectivity

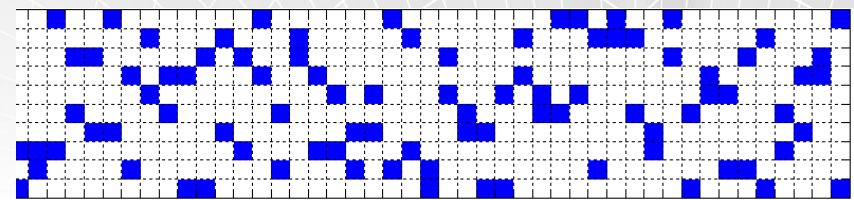
$$\text{overloading factor} = \frac{\text{UEs/data layers}}{\text{number of resources}}$$



FN:4; VN:6; OV=150%

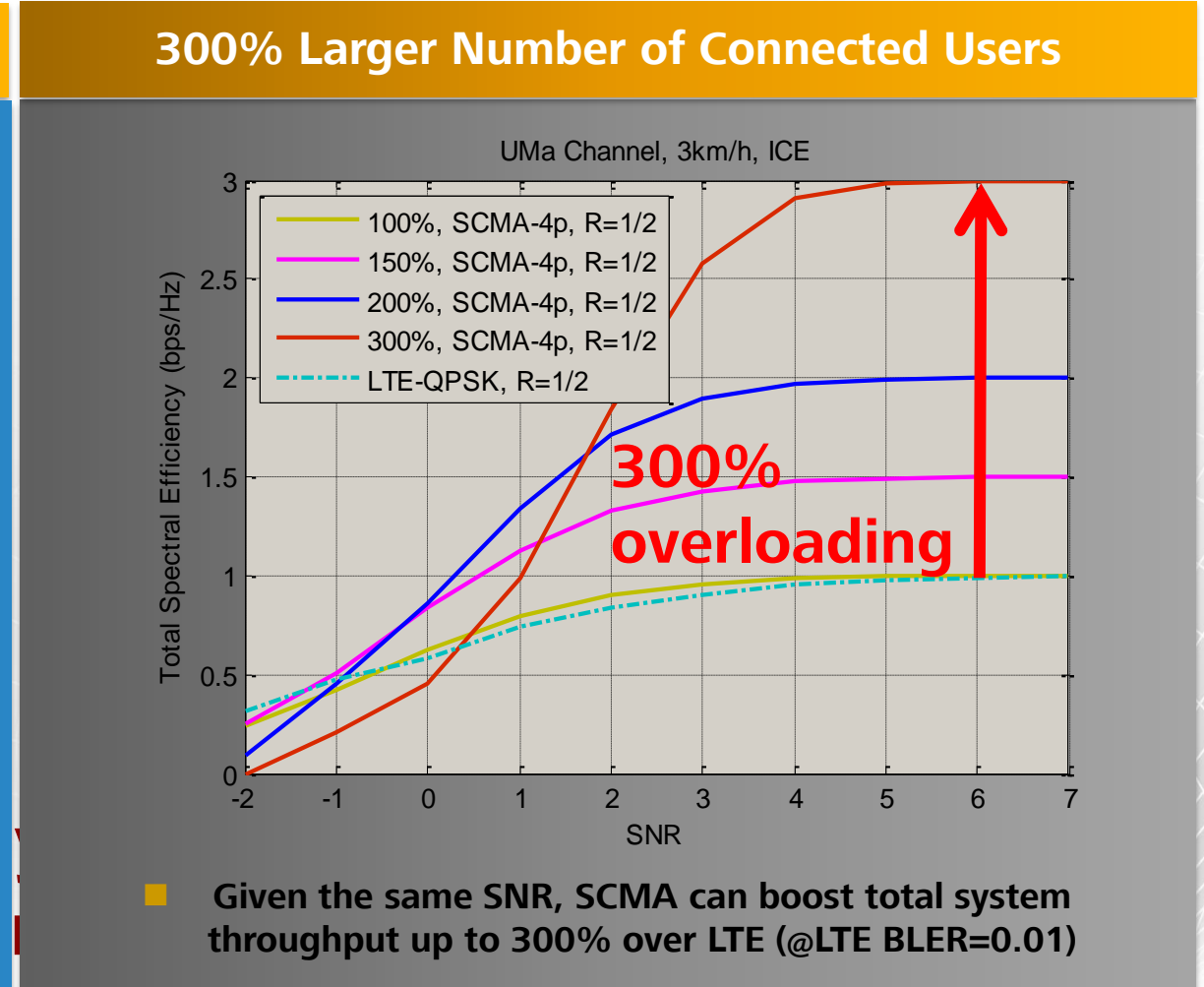
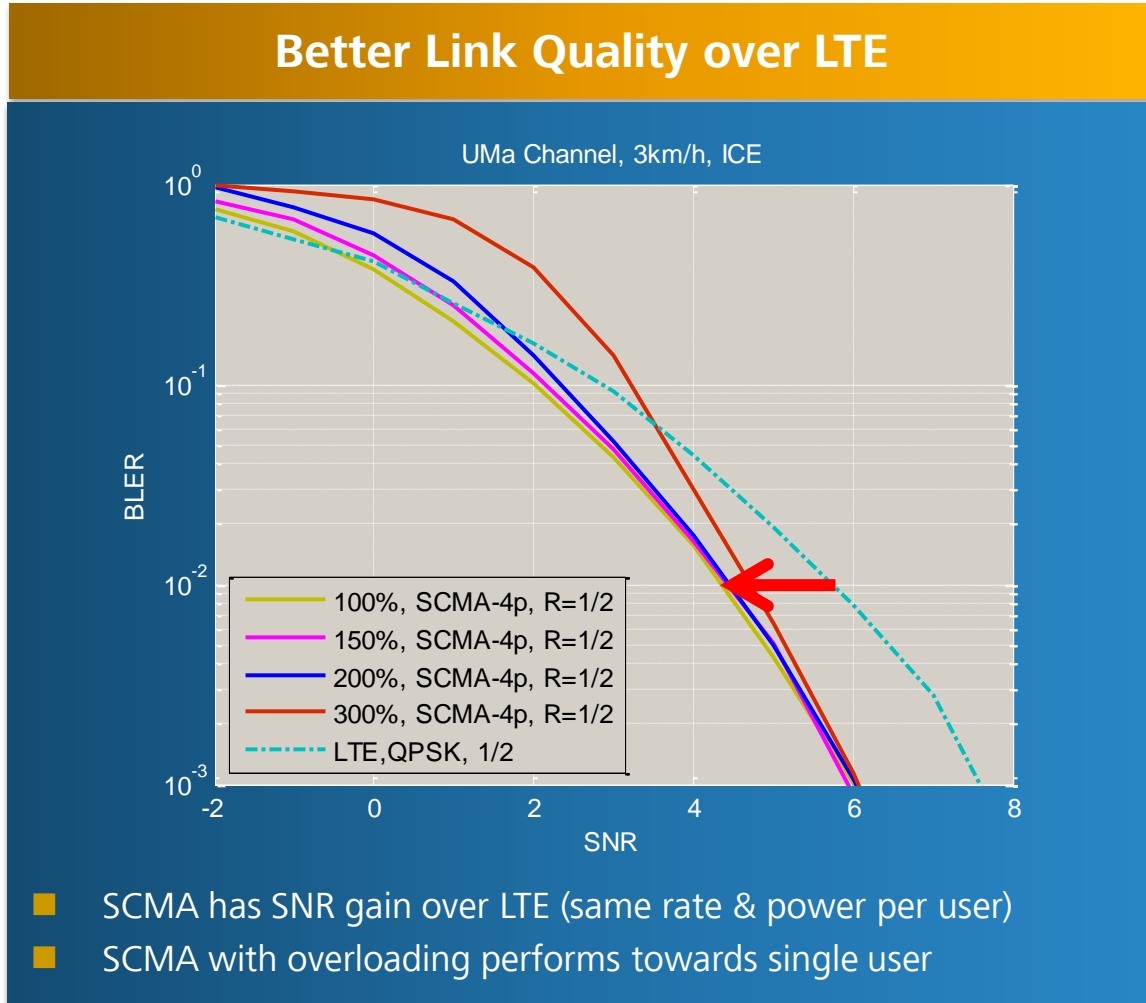


FN:6; VN:15; OV=250%



FN:10; VN:45; OV=450%

# Flexible overloading to support massive connectivity



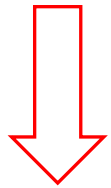
SCMA Offers Better Link Quality and 300% Larger Number of Physical Link Connections over LTE.



# Blind detection to support Grant-free transmission

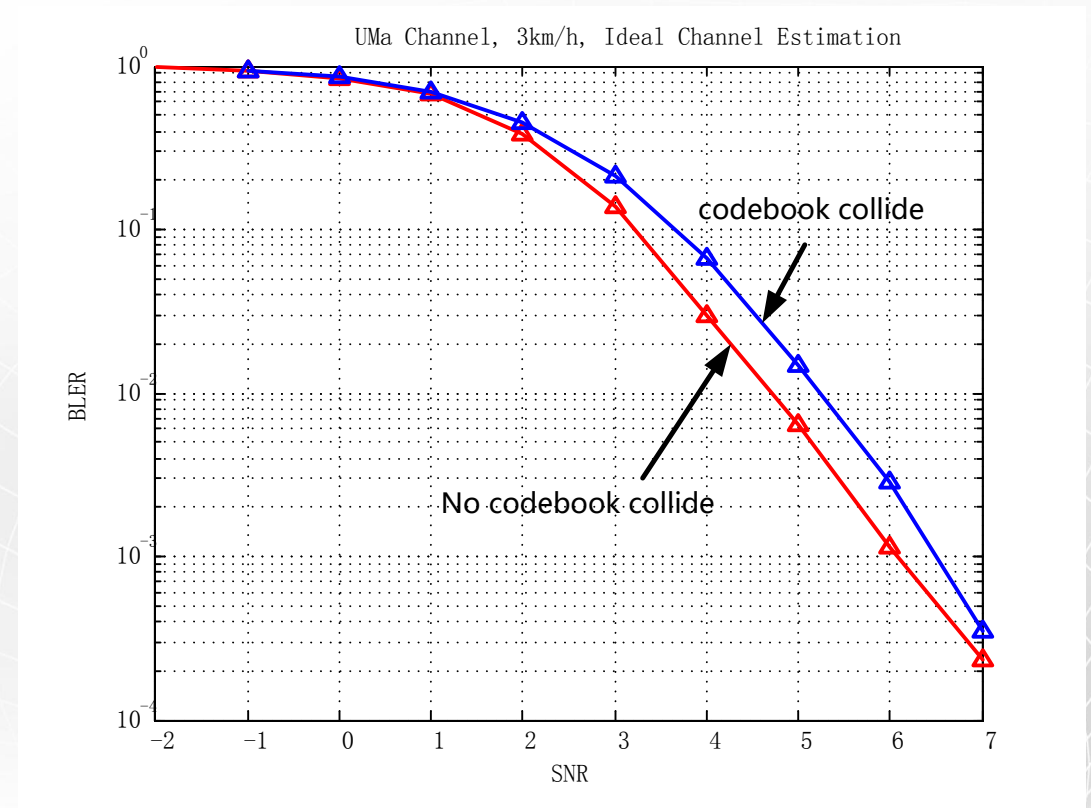
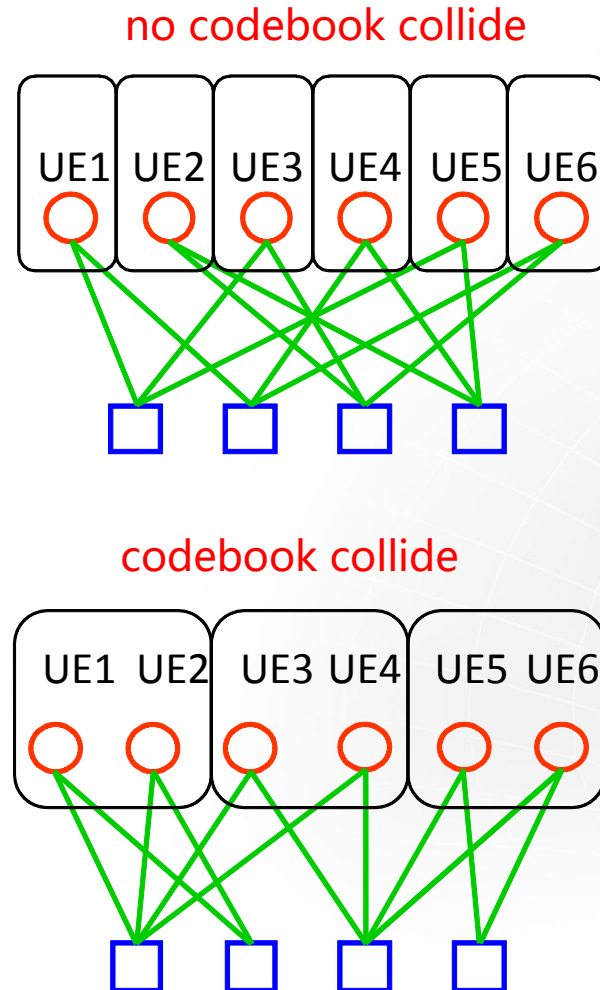
## Blind detection

- Joint detection of users' status and data;
- Robust to codebook collision.



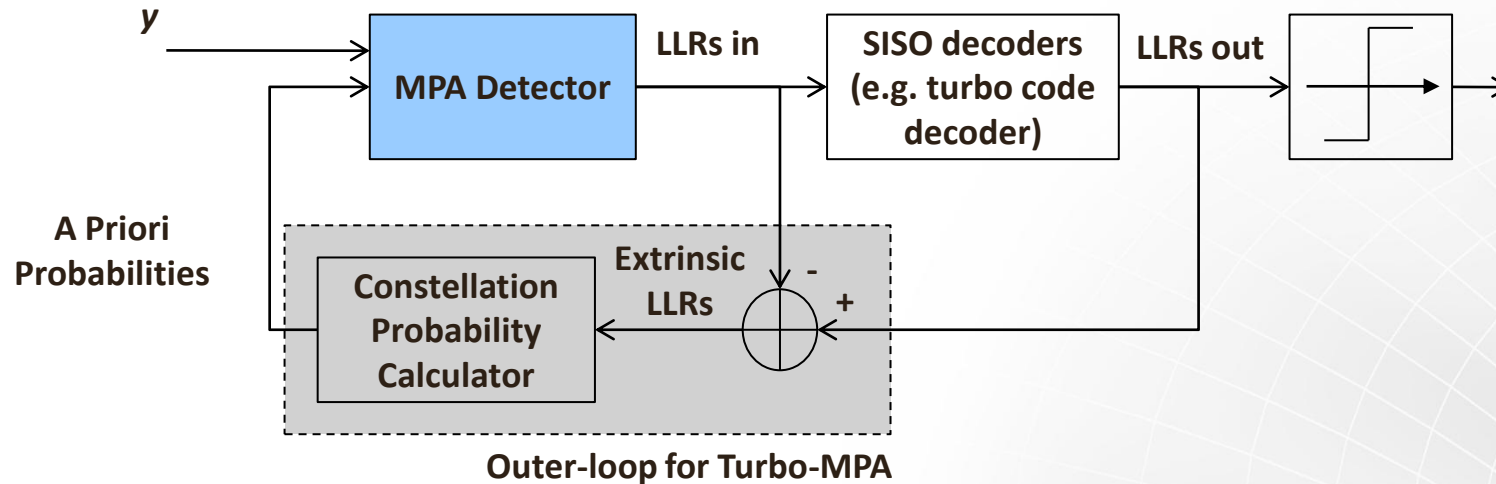
## Grant-free transmission

- No need to schedule users for uplink transmissions.

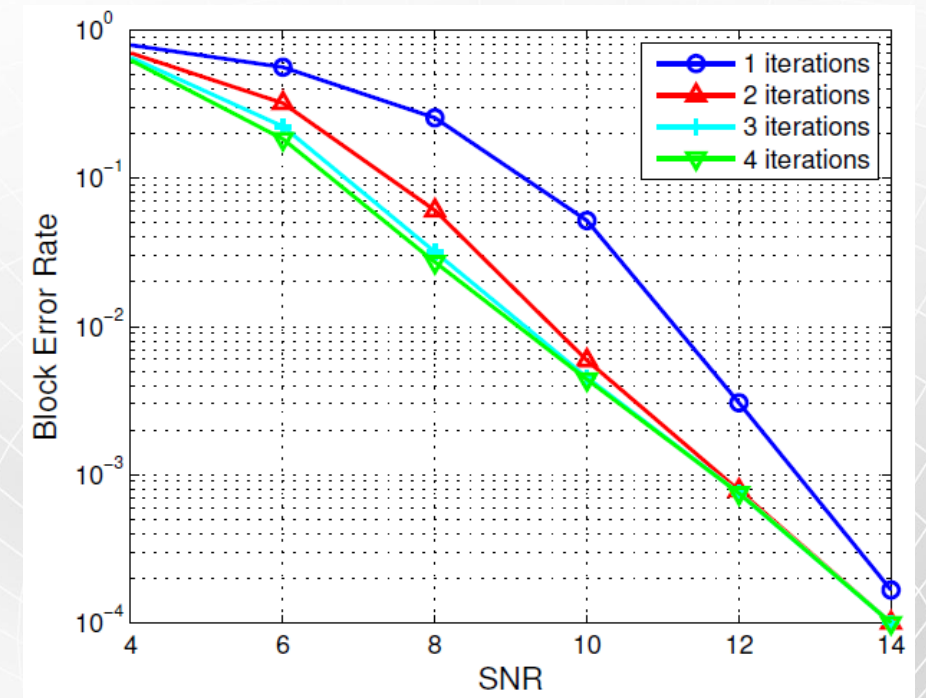


when the codebook collides, the performance loss is less than 0.5dB

# Outer-loop Turbo MPA to enhance the performance



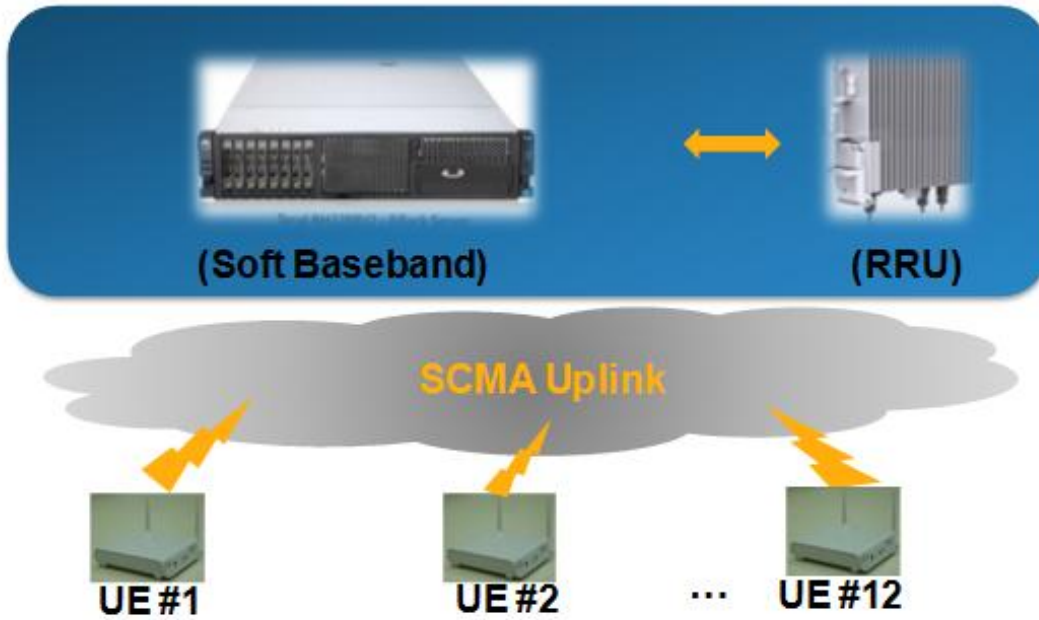
The iterative detection between MPA decoder and Turbo decoder can significantly improve the performance.



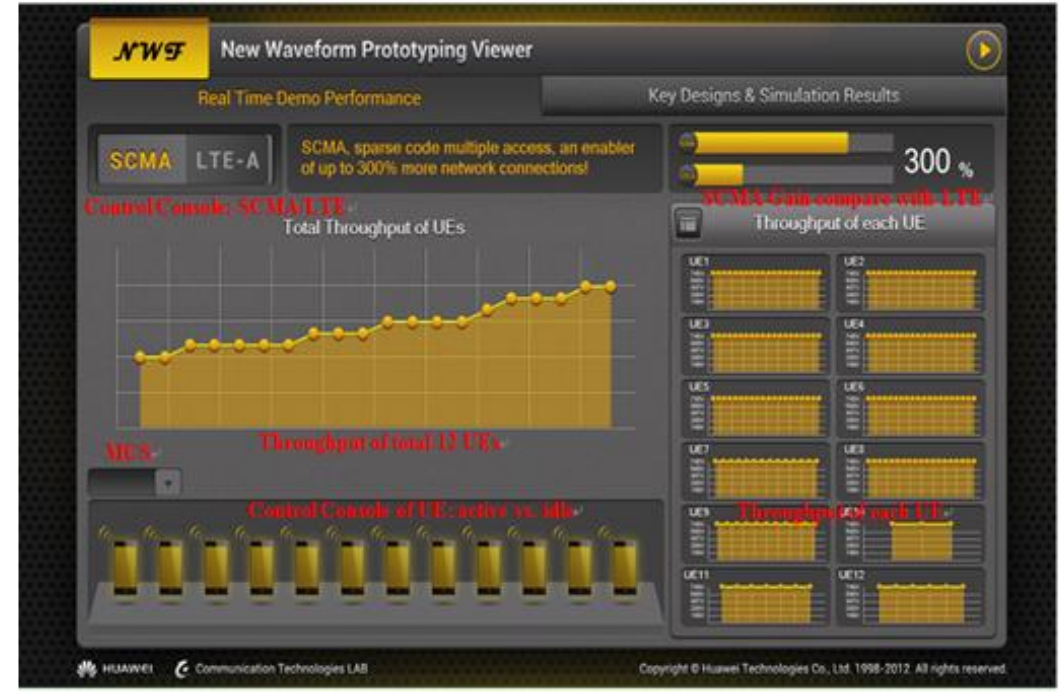
**about 2 dB SNR gain at the BLER of  $10^{-2}$  with 4 iterations**

# **REAL-TIME SCMA DEMO IN FIELD**

# Base Station



Parameters	Contents
Frame Structure	TDD, Uplink, LTE R10
Mode	SCMA over F-OFDM
Carrier Frequency	2.6GHz
System Bandwidth	20MHz
No. of UEs @4RB (20 byte small packets for each UE)	LTE baseline: 4 SCMA: up to 12
Total UE Tx Power	23dBm (Max.)
Rx Antenna Conf. of eNB	2 Rx
Tx Antenna Conf. of UE	1 Tx





Case 1.1: 6 ue in same fixed location



Case 1.2: 6 ue in different fixed location



Case 1.3: 6 ue walk around road (near)



Case 1.4: 6 ue walk around road (far)

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